

# Reusable Components of Semantic Specifications

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# **MODULARITY – A Good Thing!**

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**Our paper**

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## Our paper

- ▶ **modular framework**: component-based semantics

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- ▶ **modular framework**: component-based semantics
- ▶ **preliminary case study**: CAML LIGHT

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- ▶ developing a **language specifier's workbench**

# Component-based semantics

















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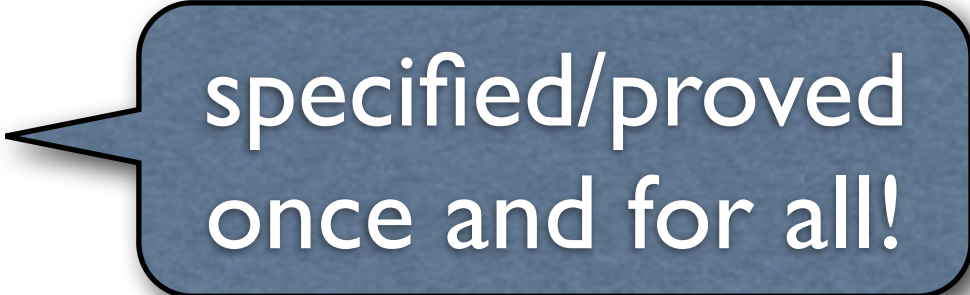
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specified/proved  
once and for all!

# Component reuse

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## ***Language construct:***

▶  $exp ::= exp ? exp : exp$



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## Translation to funcons:

▶  $expr[E_1 ? E_2 : E_3] =$   
 $\text{if-true}(expr[E_1], expr[E_2], expr[E_3])$

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## For languages with non-Boolean tests:

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## Language construct:

- ▶  $stm ::= \mathbf{if}(exp) \ stm \ \mathbf{else} \ stm$

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- ▶  $comm[\mathbf{if}(E_1) \ S_2 \ \mathbf{else} \ S_3] =$   
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destructive  
change

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## *Notation*

**if-true**(boolean, comp( $T$ ), comp( $T$ )) : comp( $T$ )

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## Notation

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## Static semantics

$$\frac{E : \text{boolean}, \quad X_1 : T, \quad X_2 : T}{\text{if-true}(E, X_1, X_2) : T}$$

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**if-true**(true,  $X_1, X_2$ )  $\rightarrow X_1$

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## Component-based semantics:

- ▶ ***translation to funcons***
  - illustrative examples
  - introduction to CAML LIGHT case study

# Funcon notation – examples

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- ▶ **comp( $T$ )** – *funcons computing values of type  $T$*

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  - *SCALA:  $\Rightarrow T$*

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## *Sorts of funcons*

- ▶ **comm** = **comp(skip)**
- ▶ **decl** – *declarations, computing environments*
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# Funcon notation – examples

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## *Types of values*

- ▶ **boolean, int, atom, ...**
- ▶ **list**( $S$ ), **map**( $S, T$ ), ...
- ▶ **array, record, tuple, ...**
- ▶ **abs**( $S, T$ )
  - **func** = **abs**(value, env), **patt** = **abs**(value, env), ...

# Funcon notation – examples

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- ▶ **abs**( $S, T$ )
  - **func** = **abs**(value, env), **patt** = **abs**(value, env), ...

## *Abstract types (language-dependent)*

- ▶ **value, env, var, store, ...**

# Funcon notation – examples

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***Control flow funcons***

– comm = comp(skip)

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▶ **seq**(skip, comp( $T$ )) : comp( $T$ )

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- ▶ **skip** : skip



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## ***Control flow funcons***

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- ▶ **seq**(skip, comp( $T$ )) : comp( $T$ )
- ▶ **skip** : skip
- ▶ **if-true**(boolean, comp( $T$ ), comp( $T$ )) : comp( $T$ )

# Funcon notation – examples

## ***Control flow funcons***

– comm = comp(skip)

- ▶ **seq**(skip, comp( $T$ )) : comp( $T$ )
- ▶ **skip** : skip
- ▶ **if-true**(boolean, comp( $T$ ), comp( $T$ )) : comp( $T$ )
- ▶ **while-true**(comp(boolean), comm) : comm

# Funcon notation – examples

## ***Control flow funcons***

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▶ **skip** : skip



value sorts

▶ **if-true**(boolean, comp( $T$ ), comp( $T$ )) : comp( $T$ )

▶ **while-true**(comp(boolean), comm) : comm

# Funcon notation – examples

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## *Binding and scoping funcons*

– decl = comp(env)

- ▶ **scope**(env, comp( $T$ )) : comp( $T$ )
- ▶ **bind-value**(id, value) : env
- ▶ **bound-value**(id) : expr

# Funcon notation – examples

## *Binding and scoping funcons*

– decl = comp(env)

- ▶ **scope**(env, comp( $T$ )) : comp( $T$ )
- ▶ **bind-value**(id, value) : env
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## *Function abstraction and application*

- ▶ **abs**(patt, expr) : func
- ▶ **apply**(func, value) : expr
- ▶ **close**(func) : comp(func)

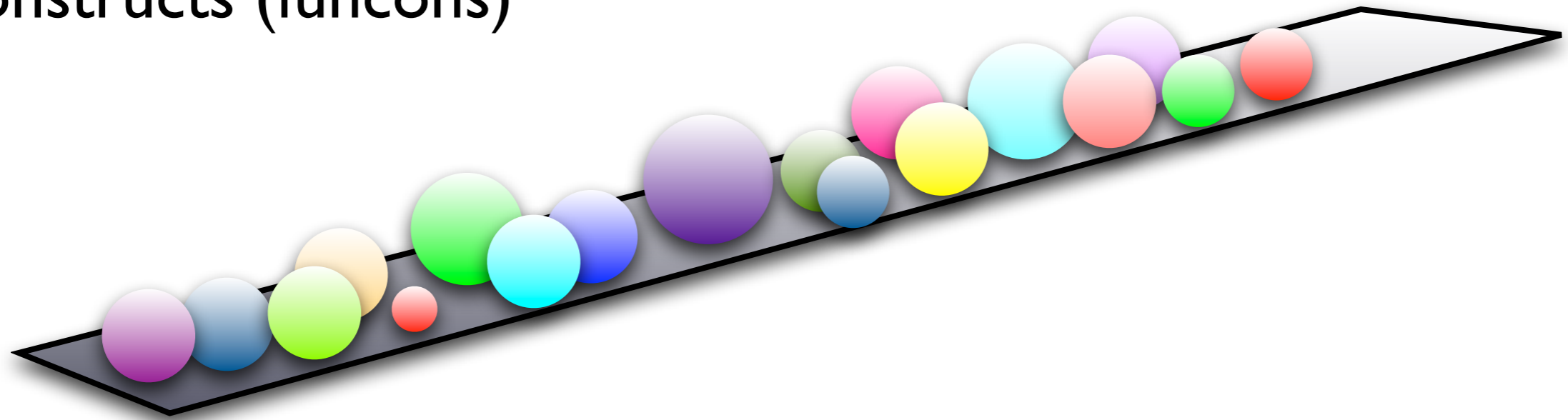
# Funcon notation – examples

## *Storing funcons*

- ▶ **allocate**(value) : comp(var)
- ▶ **assigned-value**(var) : expr
- ▶ **assign**(var, value) : comm

# Funcon notation

Fundamental programming  
constructs (funcons)





# This talk

## Reusable components:

- ▶ ***fundamental constructs (funcons)***

  - ✓ notation

  - ➔ semantics

## Component-based semantics:

- ▶ ***translation to funcons***

  - illustrative examples

  - introduction to CAML LIGHT case study

# **Funcon semantics – format**

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**Notation** (*algebraic signature*):

**Funcon**( $Sort_1, \dots$ ) :  $Sort$

# Funcon semantics – format

**Notation** (*algebraic signature*):

**Funcon**(Sort<sub>1</sub>, ...) : Sort

**Static semantics** (*context-sensitive*)

$$\frac{\Gamma_1 \vdash Var_1 : Type_1, \dots}{\Gamma \vdash \mathbf{Funcon}(Var_1, \dots) : Type}$$

# Funcon semantics – format

**Notation** (*algebraic signature*):

$$\mathbf{Funcon}(\text{Sort}_1, \dots) : \text{Sort}$$

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$$\frac{\Gamma_1 \vdash \text{Var}_1 : \text{Type}_1, \dots}{\Gamma \vdash \mathbf{Funcon}(\text{Var}_1, \dots) : \text{Type}}$$

**Dynamic semantics** (*transition system*)

$$\frac{\rho' \vdash (\text{Var}, \sigma) \rightarrow (\text{Var}', \sigma')}{\rho \vdash (\mathbf{Funcon}(\text{Term}_1, \dots), \sigma) \rightarrow (\text{Term}', \sigma')}$$

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**Notation** (*algebraic signature*):

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$$\mathbf{Funcon}(\text{Var}_1, \dots) : \text{Type}$$

**Dynamic semantics** (*transition system*)

$$\text{Var} \rightarrow \text{Var}'$$

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$$\mathbf{Funcon}(\text{Term}_1, \dots) \rightarrow \text{Term}'$$

# Funcon semantics – features

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## *Aims:*

- ▶ stable
- ▶ concise
- ▶ modular



# Funcon semantics – features

## *Aims:*

- ▶ stable
- ▶ concise
- ▶ modular

## *Means:*

- ▶ ***I-MSOS*** – implicit propagation of auxiliary entities
- ▶ ***lifting*** – implicit rules for computing expression values
- ▶ ***rule format*** – bisimulation congruence, preservation

# Funcon semantics – examples

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**Implicit!**

# Funcon semantics – examples



# Funcon semantics – examples

**seq**(skip, comp( $T$ )) : comp( $T$ )

# Funcon semantics – examples

**seq**(skip, comp( $T$ )) : comp( $T$ )

$$\frac{C : \mathbf{comm}, \quad X : T}{\mathbf{seq}(C, X) : T}$$

# Funcon semantics – examples

$$\mathbf{seq}(\text{skip}, \text{comp}(T)) : \text{comp}(T)$$
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$$\mathbf{seq}(\mathbf{skip}, X) \rightarrow X$$

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**bound-value**(id) : expr

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env  $\Gamma \vdash$  **bound-value**( $l$ ) :  $\Gamma(l)$



# Funcon semantics – examples

**bound-value**(id) : expr

env  $\Gamma \vdash$  **bound-value**( $l$ ) :  $\Gamma(l)$

env  $\rho \vdash$  **bound-value**( $l$ )  $\rightarrow$   $\rho(l)$

# Funcon semantics – examples

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**scope**(env, comp( $T$ )) : comp( $T$ )

# Funcon semantics – examples

**scope**(env, comp( $T$ )) : comp( $T$ )

$$\frac{\text{env } \Gamma \vdash D : \Gamma_1, \quad \text{env } (\Gamma_1/\Gamma) \vdash X : T}{\text{env } \Gamma \vdash \mathbf{scope}(D, X) : T}$$

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# This talk

## Reusable components:

- ▶ *fundamental constructs (funcons)*
  - ✓ notation
  - ✓ semantics

## Component-based semantics:

- ▶ ***translation to funcons***
  - ➔ illustrative examples
  - introduction to CAML LIGHT case study



# Language specifications

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## *Syntax*

- ▶ context-free
- ▶ concrete  $\leftrightarrow$  abstract

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## Syntax

- ▶ context-free
- ▶ concrete  $\leftrightarrow$  abstract

## Semantics

- ▶ *translation*  $[ \text{abstract syntax sort} ] : \mathbf{funcon\ sort}$
- ▶ specified inductively by equations
- ▶ induces both static and dynamic semantics
  - *relationship adjustable by adding ‘static funcons’*

# Component-based semantics – examples

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*Translation function*

# Component-based semantics – examples

## *Translation function*

▶  $comm[stm] : comm$

# Component-based semantics – examples

## *Translation function*

▶  $comm \llbracket stm \rrbracket : comm$

## *Translation equations*

# Component-based semantics – examples

## *Translation function*

▶  $comm[stm] : comm$

## *Translation equations*

▶  $stm ::= \{ \}$



# Component-based semantics – examples

## *Translation function*

▶  $comm[stm] : comm$

## *Translation equations*

▶  $stm ::= \{ \}$

-  $comm[ \{ \} ] = skip$

# Component-based semantics – examples

## Translation function

- ▶  $comm \llbracket stm \rrbracket : comm$

## Translation equations

- ▶  $stm ::= \{ \}$ 
  - $comm \llbracket \{ \} \rrbracket = skip$
- ▶  $stm ::= stm \ stm^+$

# Component-based semantics – examples

## Translation function

- ▶  $comm \llbracket stm \rrbracket : \mathbf{comm}$

## Translation equations

- ▶  $stm ::= \{ \}$ 
  - $comm \llbracket \{ \} \rrbracket = \mathbf{skip}$
- ▶  $stm ::= stm \ stm^+$ 
  - $comm \llbracket S_1 \ S_2 \ \dots \rrbracket = \mathbf{seq}(comm \llbracket S_1 \rrbracket, comm \llbracket S_2 \ \dots \rrbracket)$

# Component-based semantics – examples

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## *Translation functions*

- ▶  $comm \llbracket stm \rrbracket : comm$
- ▶  $expr \llbracket exp \rrbracket : expr$

# Component-based semantics – examples

## Translation functions

▶  $comm \llbracket stm \rrbracket : \mathbf{comm}$

▶  $expr \llbracket exp \rrbracket : \mathbf{expr}$

## Translation equations

▶  $stm ::= \mathbf{if} (exp) stm \mathbf{else} stm$

-  $comm \llbracket \mathbf{if} (E) S_1 \mathbf{else} S_2 \rrbracket =$   
 $\mathbf{if-true}(expr \llbracket E \rrbracket, comm \llbracket S_1 \rrbracket, comm \llbracket S_2 \rrbracket)$

▶  $stm ::= \mathbf{if} (exp) stm$

-  $comm \llbracket \mathbf{if} (E) S \rrbracket = comm \llbracket \mathbf{if} (E) S \mathbf{else} \{\} \rrbracket$

# Component-based semantics – examples

## Translation functions

- ▶  $comm \llbracket stm \rrbracket : \mathbf{comm}$
- ▶  $expr \llbracket exp \rrbracket : \mathbf{expr}$

## Translation equations

- ▶  $stm ::= id = exp ;$ 
  - $comm \llbracket I = E ; \rrbracket = \mathbf{assign}(\mathbf{bound-value}(I), expr \llbracket E \rrbracket)$
- ▶  $exp ::= id$ 
  - $expr \llbracket I \rrbracket = \mathbf{assigned-value}(\mathbf{bound-value}(I))$

# This talk

## Reusable components:

- ▶ *fundamental constructs (funcons)*
  - ✓ notation
  - ✓ semantics

## Component-based semantics:

- ▶ ***translation to funcons***
  - ✓ illustrative examples
  - ➡ introduction to CAML LIGHT case study



# Case study: CAML LIGHT

## ***A pedagogical functional programming language***

- ▶ a sub-language of CAML
  - *some constructs differ a bit from OCAML*
- ▶ similar to the Core of STANDARD ML
  - *except for order of evaluation!*
- ▶ higher-order, polymorphic, pattern-matching, ...
- ▶ references, mutable arrays, mutable record fields, ...
- ▶ abstract syntax defined in the reference manual

# Case study: CAML LIGHT

## *Introduction*

- ▶ section 3 of the paper

## *Full specification*

- ▶ available online [[www.plancomps.org/churchill2014](http://www.plancomps.org/churchill2014)]

## *(Incomplete) validation* using test programs

- ▶ parser generated from abstract syntax grammar (in SDF2)
- ▶ translation to funcons implemented (in ASF+SDF)
- ▶ interpreter (in PROLOG) generated from I-MSOS rules

## *Needs polishing and further testing...*

# Conclusion

# Conclusion

## *Funcons – A Good Thing!*

- ▶ **reusable components** of semantic specifications
- ▶ each funcon **specified once and for all**
  - *I-MSOS, lifting, implicit rules*
- ▶ optimal(?) **abstraction level**
  - *simple translations*
  - *simple rules*

# Conclusion

## *Funcons – A Good Thing!*

- ▶ **reusable components** of semantic specifications
- ▶ each funcon **specified once and for all**
  - *I-MSOS, lifting, implicit rules*
- ▶ optimal(?) **abstraction level**
  - *simple translations*
  - *simple rules*

*But further case studies are needed to prove it*

- ▶ C#, JAVA, DSLs, ...



# Appendix

# Function semantics – examples

**assigned-value**(var) : expr

$E : \mathbf{var}(T)$

---

**assigned-value**( $E$ ) :  $T$

**assigned-value**( $V$ ), store  $\sigma$   $\rightarrow$  ( $\sigma(V)$ , store  $\sigma$ )

$E \rightarrow E'$

---

**assigned-value**( $E$ )  $\rightarrow$  **assigned-value**( $E'$ )

**Implicit!**



# Funcon semantics – examples

**assign**(var, value) : expr

$$\frac{E_1 : \mathbf{var}(T), \quad E_2 : T}{\mathbf{assign}(E_1, E_2) : \mathbf{comm}}$$

$(\mathbf{assign}(V_1, V_2), \text{store } \sigma) \rightarrow (\mathbf{comm}, \text{store } \sigma[V_1 \mapsto V_2])$

$$\frac{E_1 \rightarrow E_1'}{\mathbf{assign}(E_1, E_2) \rightarrow \mathbf{assign}(E_1', E_2)}$$
$$\frac{E_2 \rightarrow E_2'}{\mathbf{assign}(E_1, E_2) \rightarrow \mathbf{assign}(E_1, E_2')}$$

**Implicit!**

# Funcon notation – examples

# **Funcon notation – examples**

***Data flow funcons***

# Funcon notation – examples

## *Data flow funcons*

- ▶ *value <: expr – computed values*

# Funcon notation – examples

## *Data flow funcons*

- ▶ *value <: expr – computed values*
- ▶ *lifted value operations*

# Funcon notation – examples

## *Data flow funcons*

- ▶ value <: expr – *computed values*
- ▶ *lifted value operations*
  - **not**(boolean) : boolean ➡  
**not**(expr ) : expr

# Funcon notation – examples

## *Data flow funcons*

- ▶ value <: expr – *computed values*
- ▶ *lifted value operations*
  - **not**(boolean) : boolean ➡  
**not**(expr ) : expr
  - **equal**(boolean, boolean) : boolean ➡  
**equal**(expr, expr) : expr

# Funcon notation – examples

## *Data flow funcons*

- ▶ value  $\leq$ : expr – *computed values*
- ▶ *lifted value operations*
  - **not**(boolean) : boolean ➡  
**not**(expr ) : expr
  - **equal**(boolean, boolean) : boolean ➡  
**equal**(expr, expr) : expr
- ▶ *use of previously computed value*



# Funcon notation – examples

## *Data flow funcons*

- ▶ value  $\leq$ : expr – *computed values*
- ▶ *lifted value operations*
  - **not**(boolean) : boolean ➡  
**not**(expr ) : expr
  - **equal**(boolean, boolean) : boolean ➡  
**equal**(expr, expr) : expr
- ▶ *use of previously computed value*
  - **supply**(expr, comp(X)) : comp(X)

# Funcon notation – examples

## *Data flow funcons*

- ▶ value  $\leq$ : expr – *computed values*
- ▶ *lifted value operations*
  - **not**(boolean) : boolean ➡  
**not**(expr ) : expr
  - **equal**(boolean, boolean) : boolean ➡  
**equal**(expr, expr) : expr
- ▶ *use of previously computed value*
  - **supply**(expr, comp(X)) : comp(X)
  - **given** : expr